STEREO Observations of Energetic Neutral Hydrogen Atoms during the 5 December 2006 Solar Flare

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We report the discovery of energetic neutral hydrogen atoms emitted during the X9 solar event of December 5, 2006. Beginning ~1 hour following the onset of this E79 flare, the Low Energy Telescopes (LETs) on both the STEREO A and B spacecraft observed a sudden burst of 1.6 to 15 MeV protons beginning hours before the onset of the main solar energetic particle (SEP) event at Earth. More than 70% of these particles arrived from a longitude within ±10° of the Sun, consistent with the measurement resolution. The derived emission profile at the Sun had onset and peak times remarkably similar to the GOES soft X-ray profile and continued for more than an hour. The observed arrival directions and energy spectrum argue strongly that the particle events <5 MeV were due to energetic neutral hydrogen atoms (ENAs). To our knowledge, this is the first reported observation of ENA emission from a solar flare/coronal mass ejection. Possible origins for the production of ENAs in a large solar event are considered. We conclude that the observed ENAs were most likely produced in the high corona and that charge-transfer reactions between accelerated protons and partially-stripped coronal ions are an important source of ENAs in solar events.

1. Introduction

In December of 2006, shortly after the launch of NASA's twin STEREO spacecraft, there was a series of four X-class flares, each with an associated solar energetic particle (SEP) event. At this time the two STEREO spacecraft were located close together near Earth, and the Low Energy Telescopes (LETs) and High Energy Telescopes (HETs) were already operational. Measured SEP time-intensity profiles are shown in Figure 1. Since the December 5 event originated near the east limb, with no direct connection along the spiral interplanetary magnetic field, most energetic particles from this event arrived >4 hours after the X-ray flare. Also seen between ~1130 – 1300 UT in Figure 1 is a small precursor to the main SEP event. This paper investigates the origin of this precursor.

The 5 December event occurred with little warning and was not as well observed as most X-class events. There are no coronal mass ejection (CME) images because SOHO was undergoing routine maintenance and the STEREO/SECCHI instruments were not yet operational. However, as RHESSI emerged from Earth shadow at ~1030 UT it observed hard X-ray and γ-ray emission near the peak in the GOES soft X-ray emission (see http://sprg.ssl.berkeley.edu/~tohban/browser/). In addition, at 1027 UT both STEREO WAVES instruments observed Type-II and Type-III radio bursts (showing that a shock

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had formed in the corona and that electrons were escaping into interplanetary space; see http://swaves.gsfc.nasa.gov).

2. Observations

Together, LET and HET measure the nuclear charge (Z) and kinetic energy of H, He and heavier nuclei up through Ni from ~2 to ~100 MeV-nucleon⁻¹. The LET detector system is composed of a double-ended array of 14 position-sensitive silicon solid-state detectors, including 10 thin (~25 micron thickness) detectors arranged in two fan-shaped arrays centered on a four-detector double-ended stack. The various detector combinations measure particle arrival directions over a 130° x 29° fan in both the front and back directions (Mewaldt et al. 2008). The HET sensor consists of a stack of ten circular silicon solid-state detectors (each 1-mm thick) with a cone-shaped single-ended field of view with 55° full angle (von Rosenvinge et al. 2008).

The LET sensors on both spacecraft are normally oriented such that the Sunward fan is parallel to the ecliptic and centered 45° west of the Sun along the nominal (Parker spiral) interplanetary magnetic field. However, during December 2006 the STEREO-B spacecraft was flying up-side down such that the LET-B Sunward fan and HET-B were centered 45° east of the Sun. As a result, the two LETs combined could measure particle arrival directions over 360° of the ecliptic plane.

The 5 December 2006 solar flare (located at E79 S06) was an X9 event, the sixth largest X-ray flare of solar cycle 23. The X-ray onset measured by NOAA's GOES-12 satellite occurred at 1019 UT with the maximum at ~1030 UT. The arrival directions of 1.6 to 15 MeV protons detected by the LETs during a 12-hour period on December 5 are shown in Figure 2. At ~1445 UT, protons, He, and heavier ions began arriving from a broad range of directions in the forward hemisphere.

Also seen in Figure 2 at 1130-1300 UT is a tight group of protons arriving over a very narrow angular range within $\pm 10^{\circ}$ of the Sun (no increase was seen in He or heavierion rates). The narrow width of the angular distribution and arrival times imply that these particles were not influenced by the magnetic field (oriented 36° to 67° from the Earth-Sun line during this interval) and we conclude that these protons must have been neutral particles (either neutrons or H atoms) while enroute to 1 AU that were converted to protons shortly before or as they were detected.

Protons in this precursor exhibited velocity-dispersion with the highest-energy particles arriving first. Assuming these particles originated at the Sun and have not lost energy enroute, we derive the emission profile at the Sun using the measured kinetic energy (E) to determine the particle velocity, $v = (2E/m)^{1/2}$ (using the proton mass for m). To compare to the X-ray time profile we plot the quantity $T_{obs} - (R_{St}/v) + 492$ seconds. Here R_{St} is the heliocentric distance of the STEREO spacecraft (0.983 AU). The added 492 seconds correspond to the light travel-time from the Sun to the STEREOs (for X-rays, v is the speed of light and we plot the time profile reported by GOES). The resulting emission profile (Figure 3) is remarkably similar to the GOES X-ray profile, confirming that the neutral particles originated in this solar event.

The distribution of the arrival directions is better illustrated in Figure 4, which includes 1.6-15 MeV protons arriving between 1015 and 1145 UT. Note the very narrow peak in the arrival distribution within $\pm 10^{\circ}$ of the Sun. The typical maximum uncertainty

in these directions is $\pm 6^{\circ}$, and most detector combinations that view the Sun were triggered during this burst.

3. Discussion

We first consider whether the LET observations could result from the decay of neutrons created when high-energy (>30 MeV) flare-accelerated protons and He underwent nuclear interactions with ambient H and He. This process has been modeled by Ramaty, Lingenfelter, and co-workers (Ramaty and Lingenfelter 1967, Hua and Lingenfelter 1987; Ramaty and Murphy 1987; Murphy et al. 2007). High-energy neutrons from a solar flare were first detected by Chupp et al. (1983, 1987).

In addition, Evenson, Meyer and Pyle (1983; here-after EMP) and Evenson et al. (1990) measured interplanetary protons from the beta-decay of neutrons from three eastern-hemisphere events. Since the neutron mean-life is only 885 seconds, most neutrons emitted from the Sun decay well inside 1 AU. However, EMP showed that for east-limb events like this one neutrons that decay on field lines connected to Earth must have decayed relatively near Earth because of shadowing by the solar surface.

In Figure 5a we compare the neutron-decay proton spectrum measured by EMP with energy spectra measured by LET and HET that include protons with derived solar emission times between 1015 and 1145 UT. All arrival directions are included and pre-event background proton rates were subtracted. Although neither HET viewed the Sun, there was a 2- σ excess of 13 to 40 MeV protons during this time interval, and possibly a small excess of 40-100 MeV protons (shown as an upper limit).

Also shown in Figure 5a is a theoretical neutron spectrum based on calculations by Hua and Lingenfelter (1987). Using their neutron spectrum emitted at 75° to the zenith we calculated the relative number of neutrons of each energy that would decay between 0.8 and 1 AU and normalized the resulting decay spectrum to the LET and HET >5 MeV intensities. Although this estimate is approximate, it is clear that at 1 AU neutron-decay proton spectra of solar-flare origin should show a significant intensity decrease below ~10 MeV due to the decay of low-energy neutrons before reaching field lines connected to STEREO. The LET spectrum below 5 MeV is inconsistent with an origin as neutron-decay protons. However, the excess 5 to 40 MeV protons following this flare may include a contribution from neutron-decay protons.

While the initial direction of a neutron-decay proton will be aligned with the neutron trajectory from the Sun, the decay proton will immediately begin to spiral around the magnetic field. In addition, pitch-angle scattering will gradually isotropize the proton pitch-angle distribution (PAD; see Ruffolo, 1990), as observed by EMP. As a result, we would expect to detect decay protons from many directions. However, >70% of the <5 MeV protons with emission times between 1015 and 1145 UT arrived from within 10° of the solar longitude, while at >5 MeV this fraction was ~23%. We conclude that neutrons were not responsible for the <5 MeV neutral emission, but could contribute at higher energy.

Energetic Neutral Atoms (ENAs) are a second possible source of proton events in LET. Unlike neutron-decay protons, which originate at various points in the interplanetary medium both ahead and behind the spacecraft, ENAs originate at the Sun and travel in

straight lines. After leaving the solar vicinity most will remain neutral enroute to 1 AU. In LET they are stripped of their electrons upon striking the thin front Kapton windows. Solar ENAs thereby preserve their original directions until detection.

ENAs have been observed from Earth's magnetosphere and other planetary magnetospheres (Hovestadt and Scholer 1976; Decker et al. 2005; Mitchell et al. 2005) and also from the heliosphere (Hilchenbach et al. 1998). They are usually attributed to processes in which energetic protons (or heavier ions) suddenly become neutral through charge-exchange and then fly off in the same direction as that of the original charged particle. Most ENA observations have been made between ~1 and a few hundred keV.

In Figure 5b we plot the fluence spectrum of the neutral burst, including only particles with arrival directions within $\pm 10^{\circ}$ of the Sun. Correcting the observed 1.8 to 5 MeV ENA fluence back to the Sun, neglecting any losses and assuming isotropic emission, we estimate that 1.8 x 10^{28} ENAs escaped from the Sun in the upward hemisphere.

The timing of the neutral-particle emission in Figure 3 is in excellent agreement with the X-ray flare, suggesting that the ENAs are produced by flare-accelerated particles. With ambient temperatures of 3 to 30 MK at the flare site (Feldman 1996), and 1 - 2 MK elsewhere in the corona, there should be no neutral H or He, and no He⁺, on which accelerated protons can charge exchange. However, neutral H atoms will also be produced by radiative recombination with ambient electrons (H⁺ + e \rightarrow H + γ) and by charge-exchange with heavier species such as O, Si, and Fe that retain some electrons at coronal temperatures.

In the absence of measured or theoretical cross sections for charge-exchange reactions of protons with partially-stripped heavy ions at MeV energies, we have estimated the charge-transfer cross section for $H^+ + O^{6+} \rightarrow H + O^{+7}$ from its inverse reaction, $H + O^{+7} \rightarrow H^+ + O^{6+}$, using the CTMC (classical trajectory Monte Carlo) method with detailed balancing (Olson and Salop 1977). There are some data for this inverse reaction <0.8 MeV (Phaneuf, Janev, and Pindzola 1987). While the simulation neglected corrections for K-shell capture by oxygen, which should enhance the high-energy yield (e.g., Stancil et al. 1999), we consider this a reasonable first-order estimate for ENA production by proton collisions with O, the most abundant coronal species heavier than He. The CTMC result can be represented as $\sigma = 1.2 \times 10^{-20} \ E^{-2.0} \ cm^2$ from 0.1 to 5 MeV, with E the proton energy in MeV. We assume that cross sections for charge exchange with other coronal species scale from our oxygen estimate as $(Z/8)^2$ (Olson and Salop 1977). For radiative recombination we use $\sigma_{rr} = 1.28 \times 10^{-25} \ E^{-2.0} \ cm^2$ (with E in MeV) based on a fit to theoretical cross sections >1 MeV (Andersen and Bolko 1990), neglecting effects of electron heating in the flare region.

Once produced, ENAs will be subject to ionization by electron and proton impact ionization and by UV. At MeV energies the electron and proton ionization cross sections are equal and can be represented as $\sigma_i = 2.3 \times 10^{-17} \times E^{-0.895}$ cm², with E the ENA energy in MeV (Barghouty 2000).

In solar γ -ray and neutron events $\sim 10^{31}$ to a few times 10^{33} protons with > 30 MeV are required to reproduce observations of γ -rays and neutrons produced by interactions of flare-accelerated particles in the solar atmosphere (Ramaty and Murphy 1987). From Figure 5a we estimate that the 5 December flare may have produced $\sim 10\%$ as many neutrons as the 5 June 1982 event, for which Hua and Lingenfelter (1987) estimated that 3.3×10^{33} protons > 30 MeV were required.

Recent solar γ -ray and neutron studies favor power-law spectra for flare-accelerated H and He with spectral indices ranging from -3.5 to -4.5 (Share and Murphy 1998; Lin et al. 2003; Murphy et al. 2007). For the 23 July 2002 event, Lin et al. (2003) derived proton spectral indices of -3.4 \pm 0.1, -3.8 \pm 0.1, and -4.0 \pm 0.5 from three γ -ray line ratios assuming a single power-law extending down to 2.5 MeV (the threshold for the Ne line). For a spectral index of -3.5 we estimate that ~3.5 x 10^{35} protons in the range 1.8 to 5 MeV were accelerated in the 5 December 2006 flare event.

We now estimate the ENA yield from this accelerated proton spectrum by assuming protons with <10 MeV slow down and stop somewhere in the solar atmosphere. Following Allison (1958), who analyzed the evolution of 2-component charge-exchange systems like H⁺ and H, we calculate the mean number of >1.8-MeV ENAs created by a proton with energy E as it slows using:

$$N_{ENA} = \int_{E}^{1.8} \sigma_{C}(E) \left[dE / dx(E) \right]^{-1} dE$$
 (1)

Here $\sigma_C = \sigma_{01}\sigma_{10}/(\sigma_{01} + \sigma_{10})$, where σ_{10} is the abundance-weighted cross section for $H^+ \rightarrow H$ (including radiative recombination and charge exchange), σ_{01} is the abundance-weighted cross section for the inverse reaction (electron and proton impact ionization), dE/dx(E) is the rate of energy loss in MeV/cm in an ionized plasma, and N_T is the number of target atoms per cm³ assuming coronal abundances (Feldman and Widing 2003). Note that since $\sigma_{10} << \sigma_{01}$, σ_C reduces to σ_{10} . For a proton starting with 5 MeV we find an average yield of ~ 0.01 ENAs before it slows to 1.8 MeV. In addition, >5 MeV protons can produce 1.8 – 5 MeV ENAs after slowing to <5 MeV. Integrating over the adopted solar-flare spectrum from 1.8 to 10 MeV we get $\sim 10^{33}$ ENAs produced with 1.8 – 5 MeV. Assuming isotropic emission, this is $\sim 30,000$ times the number needed to explain our observations if all upward-moving ENAs escape the Sun (attenuation in the solar atmosphere is considered below).

In the standard picture of a solar flare a great deal of energy is suddenly released in the corona through magnetic reconnection and energetic particles are quickly accelerated by one or more processes (e.g., Miller 1998; Aschwanden 2002). Based on studies of X-ray flares, Aschwanden (2002) concluded that the mean height of the acceleration region varies from \sim 5000 to 50,000 km, with an extreme maximum of \sim 200,000 km, corresponding to a heliocentric radius of \sim 1.3 R_S. The acceleration region produces both upward and downward-directed beams of energetic electrons and protons. Downward-directed electrons produce bremsstrahlung emission from the chromospheric footpoints of the flare, while nuclear interactions of downward-directed ions are responsible for solar γ -ray and neutron events (e.g., Lin et al. 2003).

Acceleration sites ≤ 1.3 R_S will be copious sources of ENA production, but when the overlying solar atmosphere in the direction of Earth is considered the estimated attenuation factor for a typical 3-MeV ENA produced at 1.15 to 1.3 R_S ranges from $\sim 10^{-24}$ to 10^{-13} . The attenuation factor is given by $F(R) = \exp(-\sigma_i N_R)$ where N_R (in cm⁻²) is the overlying column density of protons and electrons integrated from heliocentric distance R (at E79) to the STEREOs, using nominal coronal densities (Sittler and Guhathakurta 1999). This indicates that ENAs from the acceleration site or the chromospheric footpoints should not be detectable at Earth for east-limb flares. Indeed, for production sites ≤ 1.6 R_S

we find that not enough ENAs escape towards Earth in this event, even if all 10^{33} ENAs were produced there. Higher in the corona the estimated 3-MeV ENA attenuation toward Earth ranges from $\sim 10^{-4}$ at $1.7~R_S$ to $\sim 10^{-2}$ at $2.0~R_S$. We suggest that ENA emission in the December 5 event resulted mostly from ENAs produced beyond $\sim 1.6~R_S$.

ENA production will also occur by particles accelerated at the CME-driven shock. Using the same cross sections, coronal densities, an E^{-1} spectrum as observed at 1 AU (Mewaldt et al. 2005), and assuming all accelerated particles are concentrated near the shock, we estimate that $\sim 10^{35}$ protons with 1.8-5 MeV are needed to account for our measured ENA fluence (Figs 3 and 5b) as the shock moves from 3 R_S to 9 R_S in 35 min (assuming a 2000 km/s shock). This number of protons is comparable to the estimated source strength of 1.8-5 MeV protons from the large 28 October 2003 event (Mewaldt et al. 2005), indicating that the ENA yield from CME shock-accelerated particles alone may be inadequate. However, more realistic estimates would include the lateral spread of the shock and ENA production in higher-density material behind the shock.

These ENA yields depend on our estimated cross-sections for charge exchange with partially-stripped heavy ions, which are only first-order estimates. There are also uncertainties in the assumed solar-flare proton spectrum and in coronal densities.

4. Summary and Conclusions

This paper reports measurements of an energetic neutral-hydrogen burst from longitudes within $\pm 10^{\circ}$ of the Sun during the large 5 December 2006 solar flare. The derived solar emission profile is in excellent agreement with the soft X-ray profile if the particles traveled in a straight line from the Sun. The arrival directions, energy spectra, and timing of this neutral burst argue strongly that most of the particles (especially those <5 MeV) were energetic neutral hydrogen rather than neutrons. To our knowledge this is the first reported observation of ENAs >10 keV/nuc from a solar source.

In a flare or coronal environment energetic protons produce ENAs by radiative recombination. In addition, our rough estimates suggest that charge-exchange reactions with partially-stripped heavy ions may produce $\sim\!100$ times as many ENAs as radiative recombination. We estimate an upper limit to 1.8-5 MeV ENA production in this event of $\sim\!10^{33}$ ENAs by assuming flare-accelerated protons $<\!10$ MeV slow and stop in the solar atmosphere. By comparison, our observations indicate that $\sim\!1.8$ x 10^{28} ENAs escaped the Sun (assuming isotropic emission). Taking into account ENA losses we conclude that ENAs from the reconnection site or flare foot-points would not be observable at Earth. Rather, observations of east-limb events heavily favor ENA production beyond $\sim\!1.6$ R_S, including flare-accelerated protons that reach the high corona and particles accelerated at the CME-driven shock. More detailed models of ENA production and loss in a solar-flare/CME environment will be required to assess these and other possible ENA production sites.

In the approaching solar maximum, STEREO ENA observations from multiple points of view, coupled with models and other imaging data, can provide a new window for studying particle acceleration and transport on the Sun by revealing where and when low-energy ions interact with solar material. In particular, solar ENA observations may provide a means of investigating the poorly-known low-energy spectra of ions accelerated in solar flares.

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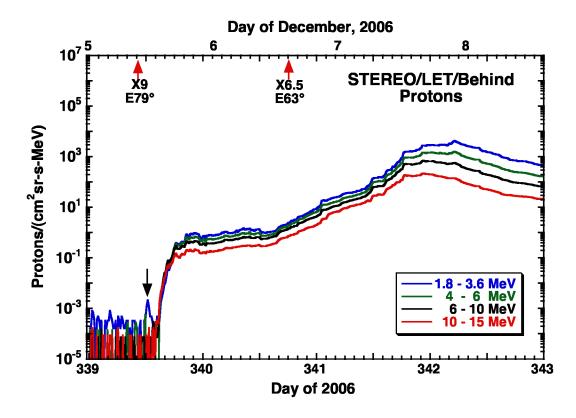


Fig. 1.—Time history of low-energy protons measured by LET-B during 5 to 8 December 2006. The onset time and location of two X-class flares are indicated. The arrow points to a burst of particles preceding the main SEP event.

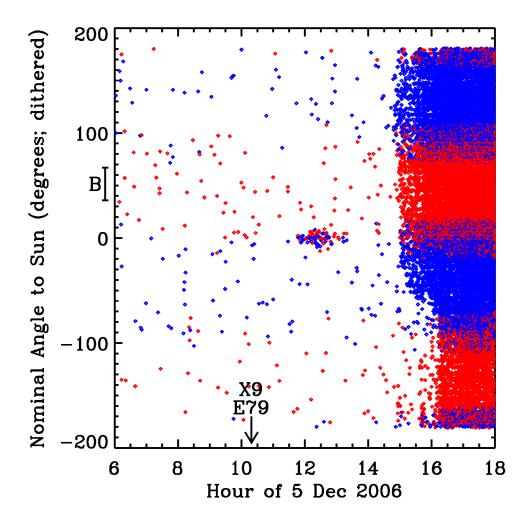


Fig. 2.—Plot of the measured angle to the Sun for individual 1.6 to 12 MeV proton events on 5 December 2006 (red = LET-A; blue = LET-B). Note the group of events within $\pm 10^{\circ}$ of the Sun from ~ 1130 UT to ~ 1350 UT, well before the SEP onset at ~ 1445 UT. The X9 flare onset is indicated. The range of magnetic field orientations connecting to the Sun between 1130 and 1350 UT is shown as a bar.

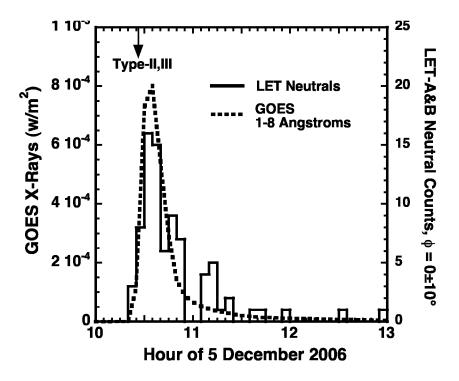


Fig. 3.—The derived emission profile of the 1.6-15 MeV neutral particle burst (in counts per 5 minutes) is compared with the GOES X-ray profile and with the onset of STEREO type-II and type-III radio bursts. The neutral-particle and X-ray emission peaks agree within ± 2.5 minutes. Both traces have 5-minute resolution.

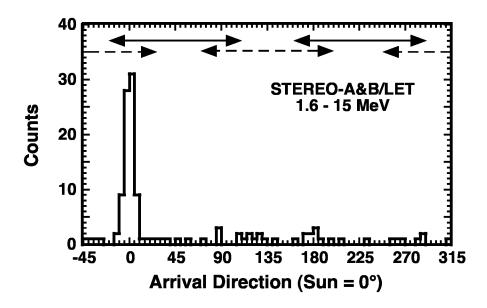


Fig. 4.—Histogram of arrival directions for LET proton events that arrived during 1015-1145 UT on December 5. The angular coverage of LET-A (solid) and LET-B (dashed) are indicated along the top.

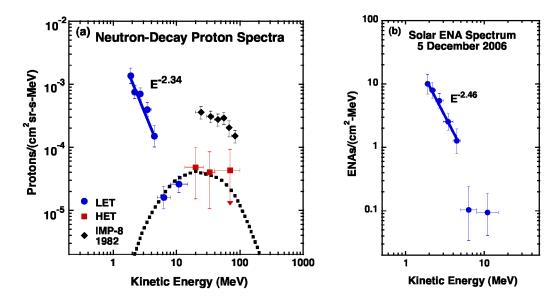


Fig. 5.—(a) Proton spectra measured by LET and HET (including protons from all arrival directions if the derived solar emission times are between 1015 and 1145 UT on December 5) are compared to neutron-decay proton spectra from IMP-8 for the 3 June 1982 event (Evenson et al. 1983). Also shown (dotted line) is a 1-AU neutron spectrum based on calculations by Hua and Lingenfelter (1987; see text). Five LET events with 1.6 to 1.8 MeV were excluded because of detection-efficiency uncertainties. (b) Spectrum of energetic neutral hydrogen measured by LET-A and LET-B during the 5 December 2006 solar event, based on detected protons with arrival directions within $\pm 10^{\circ}$ of the Sun and derived solar emission times between 1015 and 1145 UT. The >5 MeV points may also include a contribution from neutron-decay protons (see text). Note the different units in Fig. 5a and Fig. 5b.